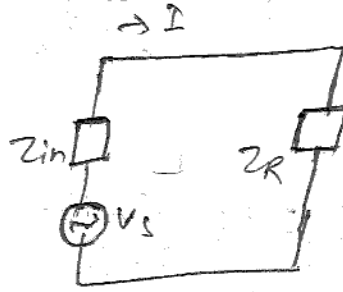
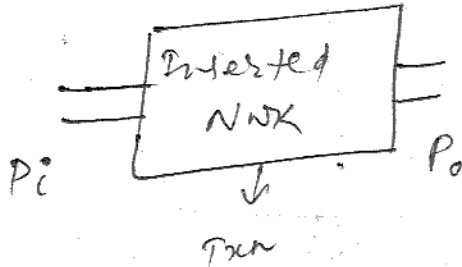


Insertion loss ( $I_L$ ): (loss of energy in tran. line)

$$I_L = 20 \log \frac{P_i}{P_o}$$



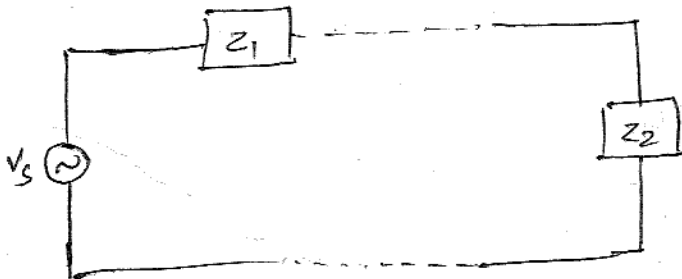
when  $Z_{in}$  &  $Z_R$  are in same phase.



J.S.  
09107111

11107111

Reflection factor and Reflection loss



$$\frac{I_2}{I_1} = \sqrt{\frac{Z_1}{Z_2}}$$

$$I_1 = \frac{V_s}{2Z_1} \quad \leftarrow \text{source end}$$

without matching  $|I_2| = I_1 \sqrt{\frac{Z_1}{Z_2}} = \frac{V_s}{2\sqrt{Z_1 Z_2}}$

with matching condition

$$|D_2| = \frac{V_s}{z_1 + z_2}$$

$$\begin{aligned} 1 \text{ neper} &= 8.686 \text{ dB} \\ 1 \text{ dB} &= 0.115 \text{ neper} \end{aligned}$$

$$\left| \frac{z_2}{z_1} \right| = K = \frac{V_s}{z_1 + z_2} \times \frac{2\sqrt{z_1 z_2}}{V_s}$$

$$\left| \frac{z_2}{z_1} \right| = \frac{2\sqrt{z_1 z_2}}{z_1 + z_2}$$

$$\text{Reflection loss} = \frac{1}{K} = \frac{z_1 + z_2}{2\sqrt{z_1 z_2}}$$

QJ

$$R = 10 \Omega/\text{km}, \quad L = 0.004 \text{ H}/\text{km}$$

$$G = 0.4 \times 10^{-6} \text{ mho}/\text{km}, \quad C = 0.008 \times 10^{-6} \text{ F}/\text{km}$$

Determine  $z_0, \alpha, \beta$  at 2 kHz

$$Z = R + j\omega L$$

$$Y = G + j\omega C$$

Soln:

$$Z = R + j\omega L \leftarrow \text{rectangular form. } [\omega = 2\pi f]$$

$$= 10 + j \times 2 \times 3.14 \times 1000 \times 0.004$$

$$= 10 + j25.12 \quad \left[ \because \text{pt} (10, 25.12) \right] \&$$

press  $\alpha$  and  $\tan$  ]

$$\boxed{Z = 27.03}$$

$$\boxed{Z = 27.03 \angle 68.3^\circ}$$

Similarly

$$Y = 50.24 \times 10^{-6} \angle 89.54^\circ$$

$$Y = 50.24 \times 10^{-6} \angle 89.54^\circ$$

$$Z_0 = \sqrt{\frac{Z}{Y}}$$

$$= \sqrt{\frac{27.04 \angle 68.3}{50.24 \times 10^{-6} \angle 89.54^\circ}}$$

$$= \sqrt{5.38 \times 10^5 \angle \left( \frac{-21.24}{2} \right)}$$

$$= \sqrt{53.8 \times 10^4 \angle (-10.62)}$$

$$\boxed{Z_0 = 7.3 \times 10^2 \angle (-10.62)}$$

$$\left[ \therefore \frac{68.3 - 89.54}{2} \right]$$

$$\boxed{Y = 0.0368 \angle 78.92^\circ}$$

14/07/11

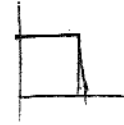
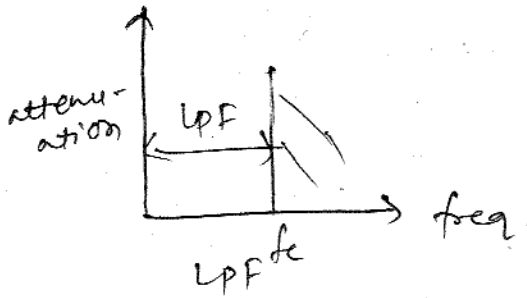
# UNIT - I

## FILTER

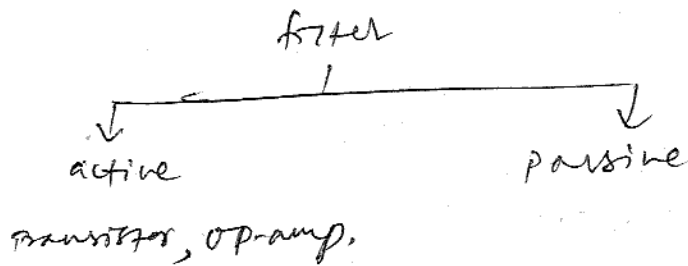
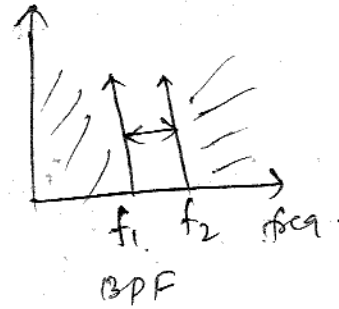
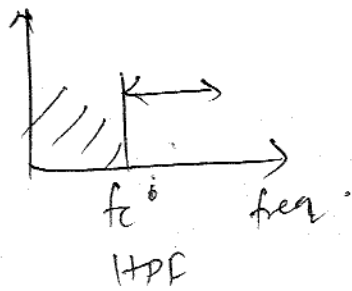
ACB

LPF, BPF,  
BSF.

Band Elimination filter



freq. passes below  $f_c$  (cut-off)



Attenuation: <sup>filter:</sup> The n/w which freely passes with the desired value of freq. & it suppresses the rest of frequencies.

Attenuation in (Nepers)

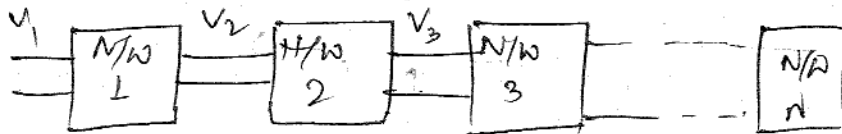
$$\text{Attenuation in (Nepers)} = \ln\left(\frac{V_1}{V_2}\right) \text{ (or)} \ln\left(\frac{I_1}{I_2}\right)$$

$$\frac{P_1}{P_2} = e^{2N}$$

$$\log e^m = m \log e$$

Attenuation (dB)

$$N = 10 \log_{10} \left( \frac{P_1}{P_2} \right)$$



$$\frac{N_1}{N_2} = \dots$$

$$\text{TOTAL Attn} = N = N_1 + N_2$$

$$\log\left(\frac{P_1}{P_2}\right) = \log e^{2N}$$

$$\log\left(\frac{P_1}{P_2}\right) = 2N \log e \quad [\because \log e = 1]$$

$$2N = \log\left(\frac{P_1}{P_2}\right)$$

$$N = \frac{1}{2} \log\left(\frac{P_1}{P_2}\right)$$

$$\text{i.e. } \boxed{N = \frac{1}{2} \ln \left( \frac{P_1}{P_2} \right)}$$

$$N_1 = \ln\left(\frac{V_1}{V_2}\right)$$

$$N_2 = \ln\left|\frac{V_2}{V_3}\right|$$

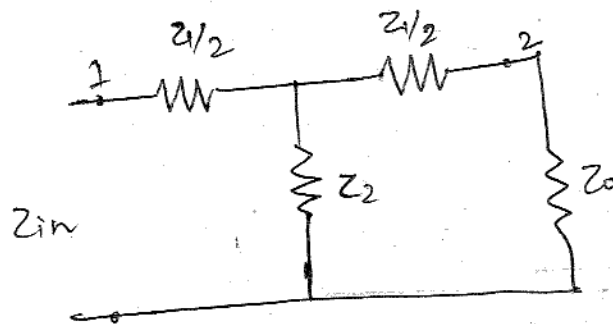
$$N = \ln\left(\frac{V_1}{V_2}\right) + \ln\left(\frac{V_2}{V_3}\right)$$

$$= \ln\left(\frac{V_1}{V_2} \times \frac{V_2}{V_3}\right) = \ln\left(\frac{V_1}{V_3}\right)$$

$$N = \ln\left(\frac{V_1}{V_3}\right)$$

## Characteristic Impedance of T-section

### Symmetrical Networks:



$$Z_{in} = \boxed{Z_{in} = Z_0} \text{ (for symmetric H/W)}$$

~~$Z_0$~~

$$Z_{0T} = \sqrt{z_1 z_2 + \frac{z_1^2}{4}}$$

$$Z_{in} = \frac{z_1}{2} + z_2 \parallel \frac{z_1}{2} (z_1/2 + z_0)$$

$$Z_{in} = \frac{z_1 + z_2(z_1/2 + z_0)}{z_2 + \frac{z_1}{2} + z_0}$$

For a symmetric n/w.

$$\boxed{Z_{in} = z_0}$$

$$z_0 = \frac{z_1 + z_2(z_1/2 + z_0)}{z_2 + \frac{z_1}{2} + z_0}$$

$$z_0 = \frac{\frac{z_1}{2}(z_2 + \frac{z_1}{2} + z_0) + z_2(z_1/2 + z_0)}{z_2 + \frac{z_1}{2} + z_0}$$

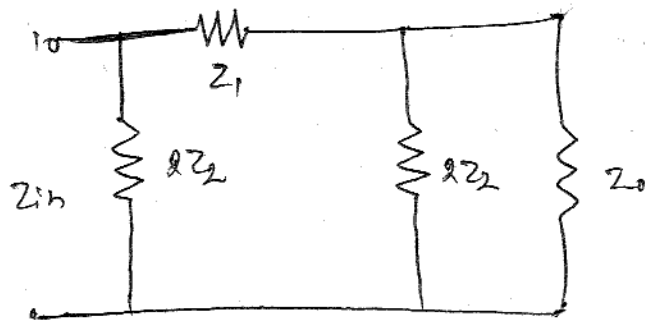
$$z_0(z_2 + \frac{z_1}{2} + z_0) = \frac{z_1 z_2}{2} + \frac{z_1^2}{4} + \frac{z_0 z_1}{2} + \frac{z_1 z_2 + z_0 z_2}{2}$$

$$z_0 z_2 + \frac{z_1 z_0}{2} + z_0^2 = \frac{z_1 z_2}{2} + \frac{z_1^2}{4} + \frac{z_0 z_1}{2} + \frac{z_1 z_2}{2} + z_0 z_2$$

$$z_0^2 = \frac{z_1 z_2}{2} + \frac{z_1^2}{4}$$

$$\boxed{z_{0n} = \sqrt{\frac{z_1 z_2}{2} + \frac{z_1^2}{4}}}$$

for T-N/w



$$Z_{in} = Z_o$$

$$Z_{in} = [(Z_o || 2Z_2) + Z_1] || 2Z_2$$

$$= 2Z_2 || \left[ Z_1 + \frac{Z_o 2Z_2}{Z_o + 2Z_2} \right]$$

$$= \frac{2Z_2 \left( Z_1 + \frac{2Z_o Z_2}{Z_o + 2Z_2} \right)}{2Z_2 + Z_1 + \frac{2Z_o Z_2}{Z_o + 2Z_2}}$$

$$\frac{2Z_2 Z_1 + \frac{4Z_o Z_2^2}{Z_o + 2Z_2}}{2Z_2 + Z_1 + \frac{2Z_o Z_2}{Z_o + 2Z_2}}$$

$$\frac{2Z_1 Z_2 + \frac{4Z_o Z_2^2}{Z_o + 2Z_2}}{2Z_2 + Z_1 + \frac{2Z_o Z_2}{Z_o + 2Z_2}}$$

$$\frac{2Z_o Z_2 + Z_o Z_1 + 2Z_1 Z_2 + 2Z_o Z_2 + 4Z_2^2}{Z_o + 2Z_2}$$

$$Z_o = \frac{2Z_o Z_2 + 4Z_2^2 + 4Z_o Z_2^2}{2Z_o Z_2 + Z_o Z_1 + 2Z_1 Z_2 + 4Z_2^2 + 2Z_o Z_2}$$

$$\cancel{4Z_o^2 Z_2 + Z_o^2 Z_1} = \cancel{2Z_o Z_2 + 4Z_2^2 + 4Z_o Z_2^2}$$

$$Z_{OT}^2 = \frac{Z_1^2 Z_2^2}{Z_o^2}$$

$\frac{2Z_2 + Z_o Z_2}{2}$

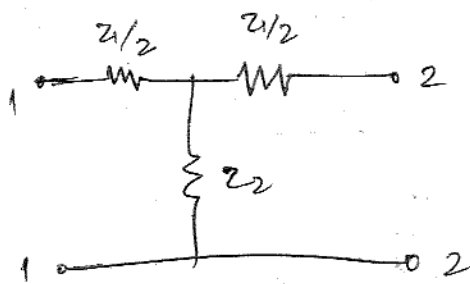
$+ Z_o Z_2$

4/w



$$Z_{OT} = \frac{Z_1 Z_2}{Z_{OT}}$$

In terms of open and short ckt.  
Impedance



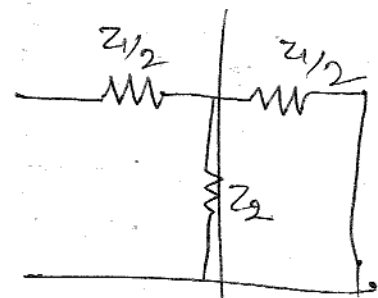
$$Z_{oc} = \frac{Z_1}{2} + Z_2 + \frac{Z_2}{2} + Z_2$$

$$Z_{oc} = 2Z_1 + 2Z_2$$

$$Z_{oc} = Z_1 + 2Z_2$$

$$Z_{oc} = \frac{Z_1}{2} + Z_2 + \frac{Z_1}{2} + Z_2$$

$$= 2Z_{1/2} + 2Z_2$$

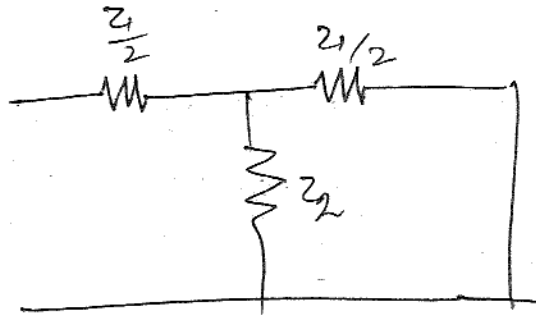


$$Z_{sc} = Z_{1/2} + \left[ \frac{Z_{1/2} \cdot Z_2}{Z_{1/2} + Z_2} \right]$$

$$= Z_{1/2} + \frac{Z_2 \cdot Z_{1/2}}{Z_{1/2} + Z_2}$$

$$= \frac{Z_{1/2}^2 + 2Z_{1/2} Z_2 + Z_2 Z_{1/2}}{Z_{1/2} + Z_2}$$

$$Z_{oc1} = Z_{oc2} = Z_{oc} = Z_{1/2} + Z_2$$



$$z_{sc} = \frac{z_1}{2} + \left[ \frac{\frac{z_1}{2} \cdot z_2}{\frac{z_1}{2} + z_2} \right]$$

$$= \frac{z_1}{2} + \frac{\frac{z_1 z_2}{2}}{\frac{z_1 + 2z_2}{2}}$$

$$= \frac{z_1}{2} + \frac{z_1 z_2}{z_1 + 2z_2}$$

$$= \frac{z_1^2 + 2z_1 z_2 + 2z_1 z_2}{2(z_1 + 2z_2)}$$

$$z_{sc} = \frac{z_1^2 + 4z_1 z_2}{2(z_1 + 2z_2)} = \frac{4 \cdot 200 \left[ \frac{z_1^2}{4} + z_1 z_2 \right]}{2(z_1 + 2z_2)} \quad \text{①}$$

$$z_{0T}^2 = z_{oc} \cdot z_{sc}$$

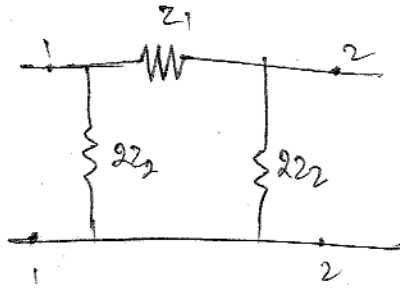
$$z_{0T} = \sqrt{z_{oc} \cdot z_{sc}}$$

$$= \frac{z_1^2/4 + z_1 z_2}{z_1/2 + z_2} = \frac{z_{0T}^2}{z_{oc}}$$

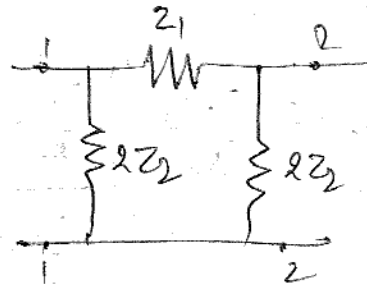
$$\therefore z_{0T} = \sqrt{z_{oc} \cdot z_{sc}} \quad //$$

12/04/11

Characteristic impedance of  $\pi$ -NW.  
w.r. to S.C. and O.C. Impedance.



for open ckt.  
impedance



For short ckt  
impedance.

O.C.  $\pi$ -Network:

$$2Z_2 \parallel (Z_1 + 2Z_2)$$

$$\frac{2Z_2 (Z_1 + 2Z_2)}{2Z_2 + Z_1 + 2Z_2}$$

S.C.  $\pi$ -Network

$$2Z_2 \parallel Z_1$$

$$\frac{2Z_2 Z_1}{2Z_2 + Z_1}$$

Now,

$$S.C \times O.C = \frac{2Z_2 Z_1}{2Z_2 + Z_1} \cdot \frac{2Z_2 (Z_1 + 2Z_2)}{Z_1 + 4Z_2}$$

$$= \frac{2Z_2 Z_1 \cdot 2Z_2 (Z_1 + 2Z_2)}{(Z_1 + 4Z_2)(Z_1 + 2Z_2)}$$

$$= \frac{4Z_1 Z_2^2}{Z_1 + 4Z_2}$$

Now, multiply and divide by  $\frac{z_1}{4}$

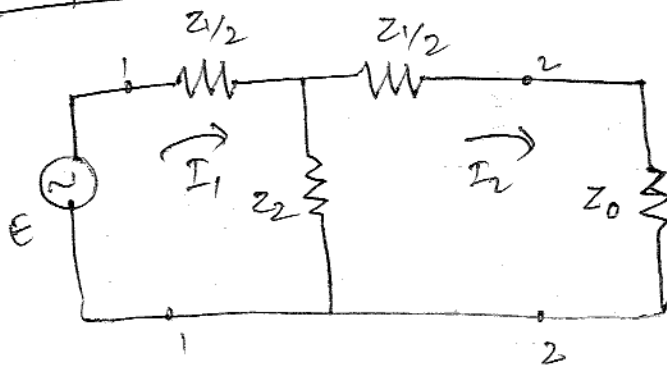
$$Z_{OT}^2 = \frac{z_1^2 z_2^2}{\frac{z_1^2}{4} + z_1 z_2}$$

$$Z_{OT} = \frac{z_1 z_2}{\sqrt{z_1 z_2 + \frac{z_1^2}{4}}}$$

$$Z_{OT} = \frac{z_1 z_2}{Z_{OT}}$$

$$\& \left[ \begin{aligned} Z_{OT} &= \sqrt{Z_{sc} \cdot Z_{oc}} \\ \text{(or)} \\ Z_{OT} &= \sqrt{Z_{si} \cdot Z_{oc}} \end{aligned} \right]$$

properties of symmetrical network



$$E = I_1 \left( \frac{z_1}{2} + z_2 \right) - I_2 z_2 \quad \text{--- (1)}$$

$$0 = I_2 (z_{1/2} + z_0 + z_2) - I_1 z_2 \quad \text{--- (2)}$$

$$I_1 z_2 = I_2 [z_{1/2} + z_0 + z_2]$$

[ sum of individual propagation const = individual const ]

$$\frac{I_1}{I_2} = \left[ \frac{z_{1/2} + z_0 + z_2}{z_2} \right]$$

$$\left[ \frac{I_1}{I_2} = e^{\gamma} \right]$$

$$\therefore \frac{z_1}{2} + z_0 + z_2 = z_2 e^{\gamma}$$

$$\textcircled{1} \quad e^{\gamma} = 1 + \frac{z_1}{z_2} + \frac{z_1^2}{2z_2^2}$$

$$e^{\gamma} = 1 + \frac{z_1}{2z_2} + \frac{\sqrt{\frac{z_1^2}{4} + z_1 z_2}}{z_2}$$

$$e^{\gamma} = 1 + \frac{z_1}{2z_2} + \sqrt{\frac{z_1^2}{4z_2^2} + \frac{z_1}{z_2}} \quad \text{--- ①}$$

$$e^{-\gamma} = 1 + \frac{z_1}{2z_2} - \sqrt{\frac{z_1^2}{4z_2^2} + \frac{z_1}{z_2}} \quad \text{--- ②}$$

$$e^{\gamma} + e^{-\gamma} = 2 \left[ 1 + \frac{z_1}{2z_2} \right]$$

$$\frac{e^{\gamma} + e^{-\gamma}}{2} = 1 + \frac{z_1}{2z_2}$$

$$\boxed{\cosh \gamma = 1 + \frac{z_1}{2z_2}}$$

$$\frac{e^{\gamma} - e^{-\gamma}}{2} = \sqrt{\frac{z_1^2}{4z_2^2} + \frac{z_1}{z_2}}$$

$$\boxed{\sinh \gamma = \sqrt{\frac{z_1^2}{4z_2^2} + \frac{z_1}{z_2}} \quad \rightarrow$$

$$\sinh \gamma = \frac{1}{z_2} \sqrt{\frac{z_1^2}{4z_2^2} + z_1 \cdot z_2}$$

$$\sinh \gamma = \frac{z_0}{z_2}$$