

UNIT-2

* Transmission Line :-

The transfer the energy from one pt to another through either transmission line or wave guide.

The electrical waves lines which transmit the electrical wave one place to another.

The example is telephone cables, electrical power signal.

* Types of transmission line

- Open wire line :- It is not insulated with any thing. Eg: telephone line and electrical signal lines.
- Cables :- These are underground lines. These are insulated by plastics or papers.
- Co-axial cable :- It has two conductor one is hollow and other is placed coaxially under the 1st material.

- Wave guides :- These are used to transmit the microwave frequency.

Range of microwave freq :- 1 GHz - 300 GHz

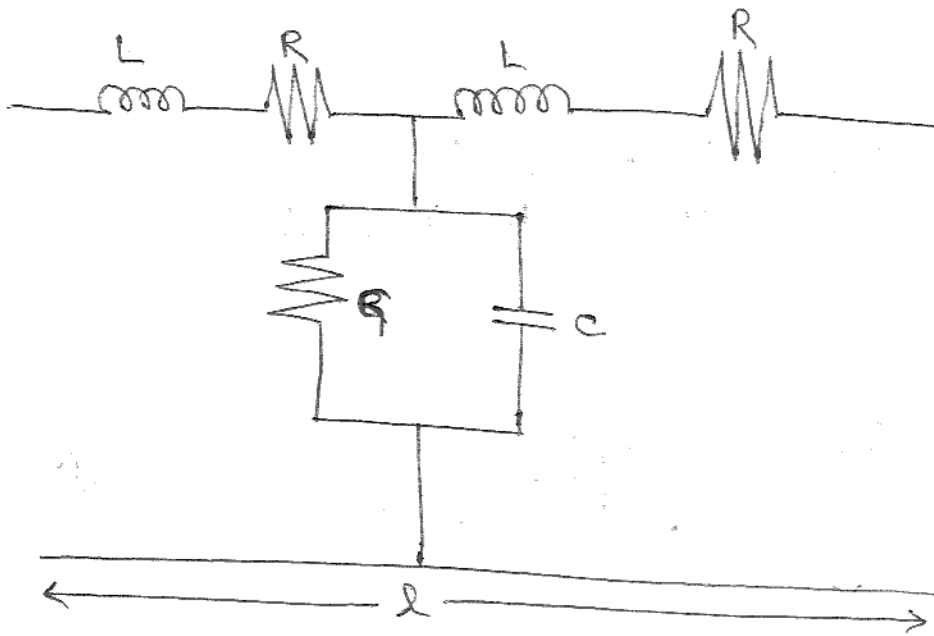
2 marks
Ex * Parameter in transmission line

- Resistance (R)
- Inductance (L)
- Capacitance (C)
- Conductance (G) = $\frac{1}{R}$

2 marks
Ex * Characteristic Impedance (Z_0)

The characteristic impedance of symmetrical n/w is the impedance measured at the i/p terminal of the 1st channel in the chain of infinite n/w in cascade and it is represented by Z_0 .

★ Equivalent circuit of Transmission Line



The parameters R , L , C and G are distributed through out the transmission line.

The serial impedance ~~by the~~ of the eq ckt is represented by

$$Z = R + j\omega L$$

The shunt ~~impedance~~ admittance is represented by

$$Y = G + j\omega C$$

When the length is l then,

$$Z_1 = (R + j\omega L) l$$

$$Y_1 = (G + j\omega C) l$$

We know that

$$Z = \frac{1}{Y}$$

$$Z_2 = \frac{1}{Y_1} = \frac{1}{(G + j\omega C)l}$$

$$Z_0 = \sqrt{\frac{Z_1^2}{4} + Z_1 Z_2} \quad \text{--- (1)}$$



Char. impe of total r/w

$$Z_0 = \sqrt{\frac{(R + j\omega L)^2 l^2}{4} + \frac{(R + j\omega L)l}{(G + j\omega C)l}}$$

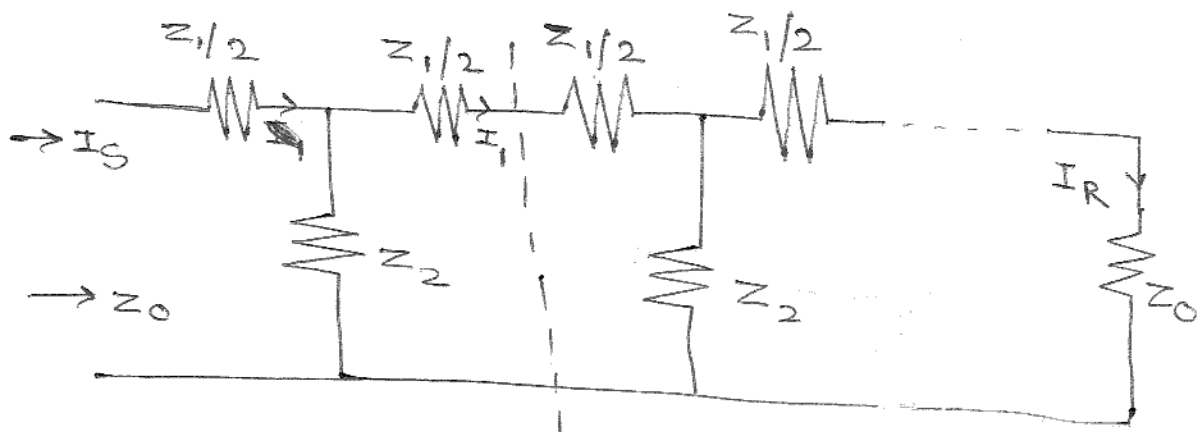
$$= \sqrt{\frac{(R + j\omega L)^2 l^2}{4} + \frac{R + j\omega L}{G + j\omega C}}$$

Let us assume length is very short

So, $l = 0$

$$\therefore Z_0 = \sqrt{\frac{R + j\omega L}{G + j\omega C}} = \sqrt{\frac{Z}{Y}}$$

★ Transmission lines as cascaded T section.



Here,

I_S = sending current

I_R = receiving current

The sending current

$$I_S = I_R e^{n\gamma}$$

where

n = no. of network

γ = proportionality propagation constant

$$\gamma = \alpha + j\beta$$

where

α = attenuation (loss)

β = phase shift

The receiving current at 1st r/w I_1

$$I_1 = I_S \times \frac{Z_2}{Z_{1/2} + Z_0 + Z_2}$$

$$\frac{I_S}{I_1} = \frac{Z_{1/2} + Z_0 + Z_2}{Z_2}$$

WKT

$$\frac{I_S}{I_R} = e^{n\gamma}$$

$$\therefore \frac{I_S}{I_1} = e^{\gamma}$$

$$\therefore e^{\gamma} = 1 + \frac{Z_0}{2} + \frac{Z_{1/2}}{Z_2}$$

For 2nd r/w

$$\frac{I_1}{I_2} = 1 + \frac{Z_0}{2} + \frac{Z_{1/2}}{Z_2}$$

Taking two r/w

$$\frac{I_S}{I_2} = \frac{I_S}{I_1} \times \frac{I_1}{I_2} = e^{2\gamma}$$

$$\therefore \frac{I_S}{I_R} = e^{n\gamma}$$

$$\frac{I_{R-1}}{I_R} = e^{(\alpha-1)l}$$

2 marks

Ans

★ Propagation constant (γ)

It is defined, as the natural logarithm of the ratio of sending end current or voltage to receiving end current or voltage.

$$\gamma = \ln \frac{I_S}{I_R} \quad \text{or,}$$

$$\gamma = \ln \frac{V_S}{V_R}$$

$$\gamma = \alpha + j\beta$$

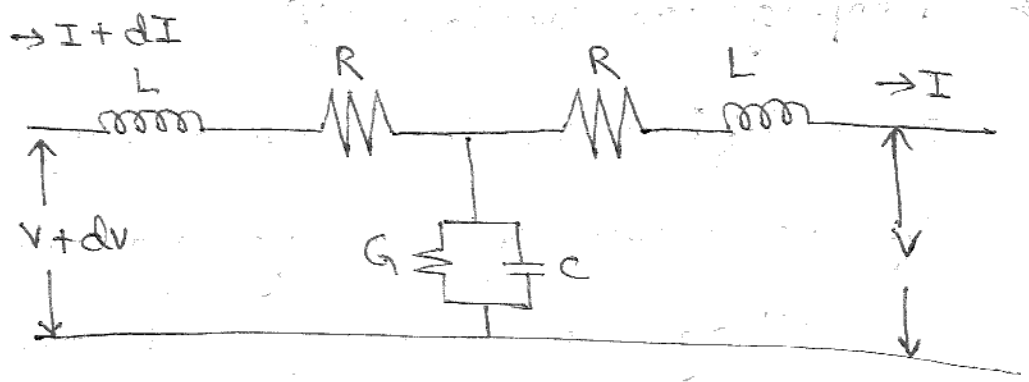
It is also known as

$$\gamma = \sqrt{ZY}$$

$$= \sqrt{(R + j\omega L)(G + j\omega C)}$$

* The general solution Transmission line
or

Transmission Line Equation



L , R , C and G are transmission line parameter.

The series impedance is

$$Z = R + j\omega L$$

The shunt admittance of the line

$$Y = G + j\omega C$$

consider the transmission line is having some distance dx .

~~consider the~~ The impedance will be

$$(R + j\omega L) dx$$

The shunt admittance will be

$$(G + j\omega C) dx$$

V, I is the output voltage and current of the trans. line.

The potential difference b/w two ends

$$V + dV - V = I(R + j\omega L)dx$$

$$\frac{dV}{dx} = I(R + j\omega L)$$

$$\frac{dV}{dx} = IZ \quad \text{--- (1)}$$

The current diff into ip and o/p of the line

$$I + dI - I = V(G + j\omega C)dx$$

$$\frac{dI}{dx} = VY \quad \text{--- (2)}$$

diff eq (1) w.r.t. x

$$\frac{d^2V}{dx^2} = (R + j\omega L) \frac{dI}{dx}$$

$$\frac{d^2V}{dx^2} = (R + j\omega L)(G + j\omega C)V \quad \text{--- (3)}$$

lly, diff. (2) w.r.t. x

$$\frac{d^2I}{dx^2} = (G + j\omega C) \frac{dV}{dx}$$

$$\therefore \frac{d^2I}{dx^2} = (G + j\omega C)(R + j\omega L)I \quad \text{--- (4)}$$

We know that

$$\gamma = \sqrt{(R + j\omega L)(G + j\omega C)} = \sqrt{ZY}$$

Sub the value of V in (3) and (4)

$$\frac{d^2 V}{dx^2} = \gamma^2 V$$

$$\frac{d^2 I}{dx^2} = \gamma^2 I$$

$$(m^2 - \gamma^2)V = 0$$

$$m = \pm \gamma$$

Also,

$$(m^2 - \gamma^2)I = 0$$

$$m = \pm \gamma$$

$$V = A e^{\gamma x} + B e^{-\gamma x} \quad \text{--- (5)}$$

$$I = C e^{\gamma x} + D e^{-\gamma x} \quad \text{--- (6)}$$

where, A, B, C, D are arbitrary constant.

Again, diff (5) w.r. to x

$$\frac{dV}{dx} = A\gamma e^{\gamma x} - B\gamma e^{-\gamma x}$$

$$\text{From (1), } \frac{dV}{dx} = IZ$$

$$\text{So, } IZ = A\gamma e^{\gamma x} - B\gamma e^{-\gamma x}$$

$$\gamma = \sqrt{ZY}$$

$$\therefore I_z = A \sqrt{ZY} e^{\sqrt{ZY}x} - B \sqrt{ZY} e^{-\sqrt{ZY}x}$$

$$I = A \sqrt{\frac{Y}{Z}} e^{\sqrt{ZY}x} - B \sqrt{\frac{Y}{Z}} e^{-\sqrt{ZY}x} \quad \text{--- (7)}$$

lly, diff eq (6) w.r. to $x =$

$$\frac{dI}{dx} = c\gamma e^{-\gamma x} - D\gamma e^{-\gamma x}$$

$$V \times \gamma = c\gamma e^{\gamma x} - D\gamma e^{-\gamma x}$$

$$V\gamma = c\sqrt{ZY} e^{\sqrt{ZY}x} - D\sqrt{ZY} e^{-\sqrt{ZY}x}$$

$$V = c\sqrt{\frac{Z}{Y}} e^{\sqrt{ZY}x} - D\sqrt{\frac{Z}{Y}} e^{-\sqrt{ZY}x} \quad \text{--- (8)}$$

If the transmission line is short line

$x=0$ and replace the value $I = \frac{V_R}{I_R}$

$$V = V_R \quad V = V_R$$

These condition are applied to (5) and

(6)

$$V_R = A + B \quad \text{--- (9)}$$

$$I_R = C + D \quad \text{--- (10)}$$

Same condition is applied to (7) and (8)

$$I_R = A \sqrt{\frac{Y}{Z}} - B \sqrt{\frac{Y}{Z}} \quad \text{--- (11)}$$

$$V_R = C\sqrt{\frac{Z}{Y}} - D\sqrt{\frac{Z}{Y}} \quad \text{--- (12)}$$

Take,

$$\sqrt{\frac{Z}{Y}} = x$$

$$\Rightarrow \frac{1}{x} = \sqrt{\frac{Y}{Z}}$$

So,

$$I_R = \frac{A}{x} - \frac{B}{x} = \frac{1}{x}(A-B)$$

compare the above eq with eq (10)

$$C + D = \frac{1}{x}(A-B) \quad \text{--- (12)}$$

$$Cx + Dx = A - B \quad \text{--- (13)}$$

lly,

$$V_R = Cx - Dx$$

compare the above eq with eq (9)

$$A + B = Cx - Dx \quad \text{--- (14)}$$

$$A - B = Cx + Dx \quad \text{--- (13)}$$

Adding (13) and (14) we get

$$2A = 2Cx$$

$$A = Cx$$

Subtracting (13) and (14) we get

$$2B = -2Dx$$

$$B = -Dx$$

Sub the value of A and B in eq (9)

$$V_R = A + B = Cx - Dx \quad \text{--- (15)}$$

From eq (10) $I_R = C + D$

mult by x in eq (10)

$$I_R x = Cx + Dx \quad \text{--- (16)}$$

Adding eq (15) and (16)

$$V_R + I_R x = 2Cx$$

$$2C = I_R + \frac{V_R}{x}$$

$$C = \frac{I_R}{2} + \frac{V_R}{2x}$$

$$C = \frac{I_R}{2} + \frac{V_R}{2} \sqrt{\frac{Y}{Z}} \quad \text{--- (17)}$$

Subtracting eq (15) and (16)

$$-2Dx = V_R - I_R x$$

$$2Dx = I_R x - V_R$$

$$D = \frac{I_R}{2} - \frac{V_R}{2x} = \frac{I_R}{2} - \frac{V_R}{2} \sqrt{\frac{Y}{Z}}$$

--- (18)

Sub. the value

$$A = Cx$$

$$A = \frac{I_R}{2} x + \frac{V_R}{2} \sqrt{\frac{Y}{Z}} \cdot x$$

$$A = \frac{V_R}{2} + \frac{I_R}{2} \sqrt{\frac{Z}{Y}} \quad \text{--- (19)}$$

$$B = -Dx$$

$$B = -\frac{I_R}{2} + \frac{V_R}{2} \sqrt{\frac{Y}{Z}} \cdot x$$

$$= \frac{V_R}{2} - \frac{I_R x}{2}$$

$$B = \frac{V_R}{2} - \frac{I_R}{2} \sqrt{\frac{Z}{Y}} \quad \text{--- (20)}$$

Replace $\sqrt{\frac{Z}{Y}}$ by z_0

The characteristic eq z_0 will be

from ohm's law

$$V_R = I_R Z_R \quad \therefore I_R = \frac{V_R}{Z_R}$$

$$z_0 = \sqrt{\frac{Z}{Y}}$$

$$A = \frac{V_R}{2} + \frac{V_R}{2Z_R} \cdot z_0 = \frac{V_R}{2} \left(1 + \frac{z_0}{Z_R}\right) \quad \text{--- (21)}$$

$$B = \frac{V_R}{2} - \frac{V_R}{2Z_R} \cdot z_0 = \frac{V_R}{2} \left(1 - \frac{z_0}{Z_R}\right) \quad \text{--- (22)}$$

$$C = \frac{I_R}{2} + \frac{I_R Z_R}{2} \cdot \frac{1}{Z_0}$$

$$C = \frac{I_R}{2} \left(1 + \frac{Z_R}{Z_0} \right) \quad \text{--- (23)}$$

$$D = \frac{I_R}{2} - \frac{I_R Z_R}{2} \cdot \frac{1}{Z_0}$$

$$D = \frac{I_R}{2} \left(1 - \frac{Z_R}{Z_0} \right) \quad \text{--- (24)}$$

Subst the value A, B, C and D in eq (5) and eq (6)

$$V = \frac{V_R}{2} \left(1 + \frac{Z_0}{Z_R} \right) e^{\gamma x} + \frac{V_R}{2} \left(1 - \frac{Z_0}{Z_R} \right) e^{-\sqrt{ZY} x} \quad \text{--- (25)}$$

$$I = \frac{I_R}{2} \left(1 + \frac{Z_R}{Z_0} \right) e^{\sqrt{ZY} x} + \frac{I_R}{2} \left(1 - \frac{Z_R}{Z_0} \right) e^{-\sqrt{ZY} x} \quad \text{--- (26)}$$

from eq (25)

$$V = \frac{V_R}{2} e^{\sqrt{ZY} x} + \frac{V_R}{2} \frac{Z_0}{Z_R} e^{\sqrt{ZY} x} +$$

$$\frac{V_R}{2} e^{-\sqrt{ZY} x} - \frac{V_R}{2} \frac{Z_0}{Z_R} e^{-\sqrt{ZY} x}$$

(21)

(22)

$$V = \frac{V_R}{2} \left[\frac{e^{\sqrt{ZY}x} + e^{-\sqrt{ZY}x}}{2} \right] + \frac{V_R Z_0}{Z_R} \left[\frac{e^{\sqrt{ZY}x} - e^{-\sqrt{ZY}x}}{2} \right]$$

Put $V_R = I_R Z_R$

$$V = V_R \left[\frac{e^{\sqrt{ZY}x} + e^{-\sqrt{ZY}x}}{2} \right] + I_R Z_0 \left[\frac{e^{\sqrt{ZY}x} - e^{-\sqrt{ZY}x}}{2} \right]$$

$$V = V_R \cosh \sqrt{ZY}x + I_R Z_0 \sinh \sqrt{ZY}x$$

— (27)

From (26)

$$I = \frac{I_R}{2} e^{\sqrt{ZY}x} + \frac{I_R}{2} e^{\sqrt{ZY}x} \frac{Z_R}{Z_0}$$

$$+ \frac{I_R}{2} e^{-\sqrt{ZY}x} - \frac{I_R}{2} e^{-\sqrt{ZY}x} \frac{Z_R}{Z_0}$$

$$I = \frac{I_R}{2} \left[\frac{e^{\sqrt{ZY}x} + e^{-\sqrt{ZY}x}}{2} \right]$$

$$+ \frac{I_R Z_R}{Z_0} \left[\frac{e^{\sqrt{ZY}x} - e^{-\sqrt{ZY}x}}{2} \right]$$

$$I = I_R \cosh \sqrt{ZY}x + \frac{V_R}{Z_0} \sinh \sqrt{ZY}x$$

— (28)

These two (27) and (28) are general solution of transmission line.

* Physical Signification of General Solution

Sending impedance Z_S is the ratio of Sending voltage and sending current.

i.e.

$$Z_S = \frac{V_S}{I_S}$$

$$V_S = V_R \cosh \gamma l + I_R Z_0 \sinh \gamma l$$

where,

$$\gamma = \sqrt{ZY}$$

$$I_S = I_R \cosh \gamma l + \frac{V_R}{Z_0} \sinh \gamma l$$

$$\therefore Z_S = \frac{I_R Z_R \cosh \gamma l + I_R Z_0 \sinh \gamma l}{I_R Z_0 \cosh \gamma l + \frac{I_R Z_R}{Z_0} \sinh \gamma l}$$

where,

$$V_R = I_R Z_R$$

$$Z_S = \frac{Z_R \cosh \gamma l + Z_0 \sinh \gamma l}{Z_0 \cosh \gamma l + Z_R \sinh \gamma l}$$

$$Z_S = Z_0 \left[\frac{Z_R \cosh \gamma l + Z_0 \sinh \gamma l}{Z_0 \cosh \gamma l + Z_R \sinh \gamma l} \right]$$

when the line is terminated $Z_R = Z_0$

$$Z_S = Z_0$$

The transmission line is of infinite length
 $l = \infty$

$$Z_S = \frac{Z_0 \cosh \gamma l [Z_R + Z_0 \frac{\sinh \gamma l}{\cosh \gamma l}]}{\cosh \gamma l [Z_0 + Z_R \frac{\sinh \gamma l}{\cosh \gamma l}]}$$

$$Z_S = \frac{Z_0 [Z_R + Z_0 \tanh \gamma l]}{Z_0 + Z_R \tanh \gamma l}$$

$$l = \infty$$

$$Z_S = Z_0 \frac{Z_R + Z_0}{Z_0 + Z_R}$$

$$Z_S = Z_0$$

* Reflection Co-efficient

It is defined as the ratio of reflected voltage to the incident voltage at the receiving end. Denoted by K .

$$K = \frac{\text{Reflected voltage}}{\text{Incident voltage}} = \frac{V_R}{V_S}$$

The general voltage equation of transmission line

$$V = \left[\frac{V_R}{2} \left[\left(1 + \frac{Z_0}{Z_R}\right) e^{\gamma x} + \left(1 - \frac{Z_0}{Z_R}\right) e^{-\gamma x} \right] \right]$$

from eq (25) ↑

$$K = \frac{V_R}{2} \left[\frac{Z_R + Z_0}{Z_R} e^{\gamma x} + \frac{Z_R - Z_0}{Z_R} e^{-\gamma x} \right]$$

$$K = V_R \frac{Z_R + Z_0}{2Z_R} \left[e^{\gamma x} + \frac{Z_R - Z_0}{Z_R + Z_0} e^{-\gamma x} \right]$$

$$= \frac{V_R}{2} \frac{Z_R + Z_0}{Z_R} e^{\gamma x} - \frac{V_R}{2} \frac{Z_R - Z_0}{Z_R} e^{-\gamma x}$$

The first term $e^{\gamma x}$ represent the incident wave.

The 2nd term $e^{-\gamma x}$ represent the reflected wave.

$$K = \frac{\frac{V_R}{2} \frac{Z_R - Z_0}{Z_R}}{\frac{V_R}{2} \frac{Z_R + Z_0}{Z_R}}$$

$$K = \frac{Z_R - Z_0}{Z_R + Z_0}$$

It is also defined in the terms of ratio of reflected current to incident current but it is -ve.

If the trans. line terminated by char. impedance $Z_R = Z_0$. At that time the reflex. coeff. becomes zero.

* Wave length And Velocity Propagation

The distance travelled by the wave along the line which the phase angle is changing through 2π radian is called wave length.

$$\beta\lambda = 2\pi$$

$$\lambda = \frac{2\pi}{\beta}$$

Velocity propagation:-

W.K.T

$$\gamma = \sqrt{ZY}$$

$$\gamma = \sqrt{(R + j\omega L)(G + j\omega C)}$$

Squaring both side

$$\gamma^2 = (R + j\omega L)(G + j\omega C)$$

$$= RG + Rj\omega C + Gj\omega L - \omega^2 LC$$

$$= (RG - \omega^2 LC) + j\omega(RC + GL)$$

Here, the mini attenuation

$$L = \frac{RC}{G}$$

$$LG = RC$$

$$\gamma^2 = RG - \omega^2 LC + 2j\omega RC$$

$$\gamma^2 = RG - \omega^2 LC + j2\omega\sqrt{RCLG}$$

$$\gamma^2 = (\sqrt{RG} + j\omega\sqrt{LC})^2$$

$$\gamma = \sqrt{RG} + j\omega\sqrt{LC}$$

$$\gamma = \alpha + j\beta$$

$$\alpha = \sqrt{RG}$$

$$\beta = \omega\sqrt{LC}$$

The veloc. propagation is given by $v = \lambda f$
mult. & divi. by 2π

$$v = \frac{\lambda}{2\pi} \cdot f \cdot 2\pi$$

$$= \frac{1}{\beta} \cdot \omega$$

$$V = \frac{W}{\beta} = \frac{W}{W\sqrt{LC}} = \frac{1}{\sqrt{LC}}$$

$$V = \frac{1}{\sqrt{LC}}$$

* Distortion Line

When the received signal is always having noise and this signal is called distorted line.

It has two types :- i) Frequency dis. line
ii) Phase dis. line

Freq. distortion is due to variation of attenuation constant α .

$$\alpha = \sqrt{\frac{RG_1 - W^2 LC + \sqrt{(RG_1 - W^2 LC)^2 + W^2 (LG_1 + RC)^2}}{2}}$$

Phase distortion is due to variation of phase constant β .

$$\beta = \sqrt{\frac{1}{2} \sqrt{(R^2 + W^2 L^2)(G^2 + W^2 C^2) - (RG_1 - W^2 LC)}}$$

* Distortionless Line

The line in which there is no phase and freq. distortion is called distortionless line.

It is also represented by β .

$$\beta = \frac{\sqrt{(\omega^2 LC - RG)^2 + (\omega^2(LG + RC))^2}}{2}$$

If the transmission line is distortionless line the 2nd term is equal to $(RG + \omega^2 LC)^2$.

$$(RG + \omega^2 LC)^2 + \omega^2(LG + RC)^2 = (RG + \omega^2 LC)^2$$

$$\cancel{R^2 G^2} + \cancel{\omega^4 L^2 C^2} - \cancel{2RG\omega^2 LC} + \omega^2 L^2 G^2 + \omega^2 R^2 C^2 + \cancel{2\omega^2 LGRC} = \cancel{R^2 G^2} + \cancel{\omega^4 L^2 C^2} + 2RG\omega^2 LC$$

$$\Rightarrow \omega^2 L^2 G^2 + \omega^2 R^2 C^2 - 2RG\omega^2 LC = 0$$

$$\Rightarrow \omega^2 (LG - RC)^2 = 0$$

$$LG - RC = 0$$

$$LG = RC$$

$$\boxed{\frac{G}{C} = \frac{R}{L}}$$

condition for distortionless line

2 marks
Dr. LL

* Telephone Cable

Telephone cable line is insulated with plastic or papers. This construction results the negligible values of inductance and conductance.

- Condition for ^{le} telephone cable

$$L\omega \gg R \quad L\omega \ll R$$

and

$$G \ll C\omega$$

$$\text{Impedance } Z = R + j\omega L = R$$

$$\text{Admittance } Y = G + j\omega C = j\omega C$$

$$\text{Propagation constant } (\gamma) = \sqrt{ZY}$$

$$= \sqrt{Rj\omega C}$$

$$= \sqrt{j\omega RC}$$

$$= \sqrt{\omega RC} \angle 90^\circ$$

$$= \sqrt{\omega RC} \angle 45^\circ$$

$$= \sqrt{\omega RC} (\cos 45^\circ + j \sin 45^\circ)$$

$$= \sqrt{\omega RC} \frac{1}{\sqrt{2}} + j \frac{1}{\sqrt{2}}$$

$$\gamma = \sqrt{WRC} \cdot \frac{1}{\sqrt{2}} (1+j)$$

$$= \sqrt{\frac{WRC}{2}} + j \sqrt{\frac{WRC}{2}}$$

comp. with

$$\gamma = \alpha + j\beta$$

$$\alpha = \sqrt{\frac{WRC}{2}}$$

$$\beta = \sqrt{\frac{WRC}{2}}$$

Velocity propagation of telephone cable

$$v = \frac{w}{\beta} = \frac{w}{\sqrt{\frac{WRC}{2}}} = \sqrt{\frac{2w}{RC}}$$

characteristic impedance $Z_0 = \sqrt{\frac{Z}{Y}}$

$$Z_0 = \sqrt{\frac{R}{j\omega C}} = \sqrt{\frac{R \angle -90^\circ}{\omega C}}$$

$$Z_0 = \sqrt{\frac{R}{\omega C}} \angle -45^\circ$$

★ Reflection on a line not terminated in Z_0

If a transmission line is not terminated by Z_0 so the line is open ckt.

$$\text{i.e. } Z_R = \infty$$

$Z_R \rightarrow 0$ for short ckt or closed ckt

• General eq for transmission line

$$V = \frac{V_R}{2} \frac{Z_R + Z_0}{Z_R} \left[e^{\gamma l} + \frac{Z_R - Z_0}{Z_R + Z_0} e^{-\gamma l} \right]$$

$$I = \frac{I_R}{2} \frac{Z_R + Z_0}{Z_0} \left[e^{\gamma l} - \frac{Z_R - Z_0}{Z_R + Z_0} e^{-\gamma l} \right]$$

Here, line is not terminated by Z_0 so,

$$Z_R \neq Z_0.$$

So, the current and voltage is consist of two parts

→ Varying exponentially with +ve l .

→ Varying exponentially with -ve l .

The first component of voltage and current varying expo. with +ve l is

called as incident wave. It flows from sending into receiving wave.

The 2nd component of voltage and current varying expon. with $-ve l$ called as reflected wave. It flows through receiving end to sending end.

Separate the incident and reflected wave from general solution.

$$V_1 = \frac{V_R}{2} \frac{Z_R + Z_0}{Z_R} e^{\gamma l} \rightarrow \text{incident wave voltage} \quad \text{--- (1)}$$

$$V_2 = \frac{V_R}{2} \frac{Z_R - Z_0}{Z_R} e^{-\gamma l} \rightarrow \text{reflected wave voltage} \quad \text{--- (2)}$$

$$I_1 = \frac{I_R}{2} \frac{Z_R + Z_0}{Z_0} e^{\gamma l} \rightarrow \text{incident wave current} \quad \text{--- (3)}$$

$$I_2 = \frac{-I_R}{2} \frac{Z_R - Z_0}{Z_0} e^{-\gamma l} \rightarrow \text{reflected wave current} \quad \text{--- (4)}$$

If line is open ckt then

$$Z_R \rightarrow \infty$$

and is

$$\text{From (1)} \quad V_1 = \frac{V_R}{2} \frac{Z_R (1 + Z_0/Z_R)}{Z_R} e^{\gamma l}$$

$$V_1 = \frac{V_R}{2} e^{j\beta l}$$

This wave propagates from sending end to receiving end.

The reflected wave component

$$V_2 = \frac{V_R}{2} e^{-j\beta l}$$

This wave travels from receiving end to sending end.

If the line short ckt $l=0$ the voltage of incident wave and reflected wave are equal i.e.

$$V_1 = V_2 = \frac{V_R}{2}$$

~~For~~ When line is terminated by Z_0 without having any reflection is called smooth line.

★ Insertion loss (I_L)

It is defined as

$$I_L = 10 \log \frac{P_i}{P_o}$$

i.e.

It is the ratio of incident power to the reflected power.

where

P_L = power received from load when connected directly from source to load.

P_0 = power received by the source when the line is inserted b/w source to load.

~~Filter~~

out
rooth

Unit - 01
FILTERS

Filters

It is the electronics device which is designed to separate and pass or suppress a group of signal through a mixer of signals. And it also passes freely a desired band of frequency. While almost suppressed other band of freq.

→ Types of filters

• Active filters

They contains transistor, inductor and op amplifiers.

• Passive filters

They contain resistor, capacitor.

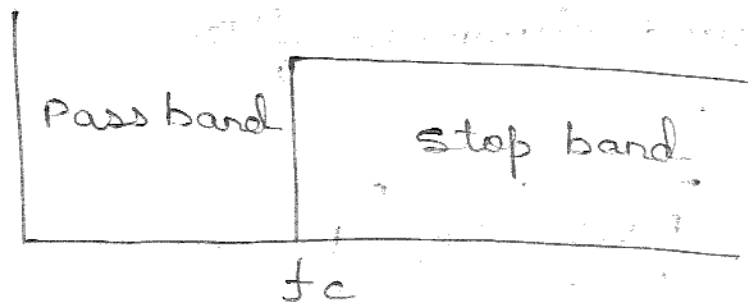
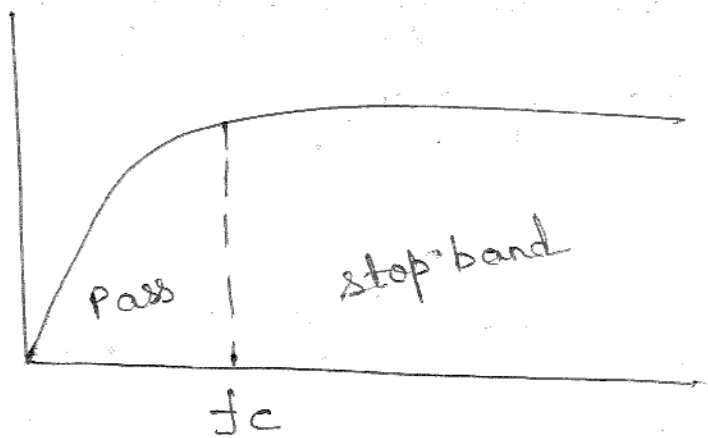
→ Types of active filters

1) Low pass filter

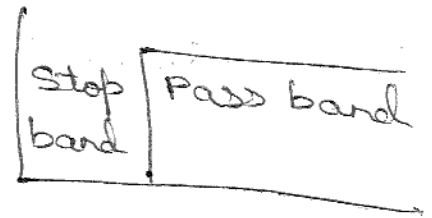
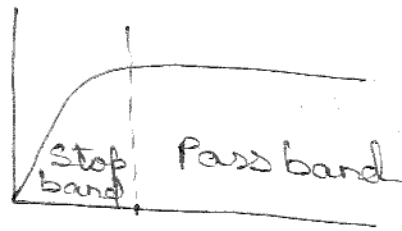
- i) High pass filter
- ii) Band pass filter
- iii) Band elimination filter

- Low pass filter

It passes all frequencies upto the cut off frequency. Also attenuates all frequencies above the cut off frequency.

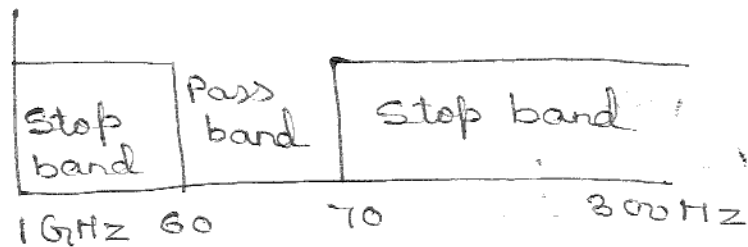


- High pass filter

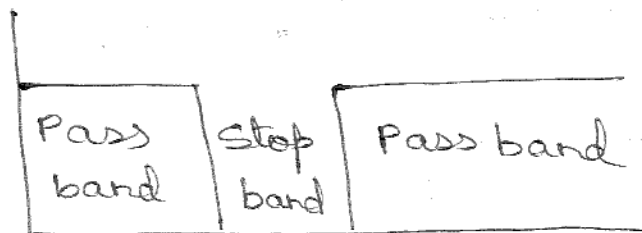


- Band pass filter

The filter passed all the frequencies b/w two cut off frequency and attenuate all other frequency.



- Band elimination filter



* Neper

It is the unit of current to voltage ratio.

or

It is defined as the natural logarithm of input voltage or current to the output voltage or current.

$$\text{Neper} = \ln \frac{V_1}{V_2} \quad \text{or} \quad \ln \frac{I_1}{I_2}$$

Similarly, the power ratio of any one electrical n/w i.e.

$$\frac{P_1}{P_2} = e^{2N}$$

where

$N = \text{Neper}$

$P_1 = \text{i/p power}$

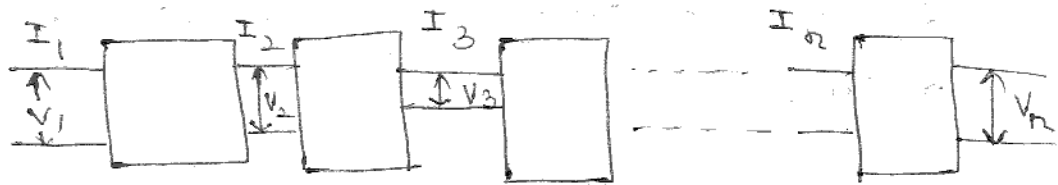
$P_2 = \text{o/p power}$

Take \ln both side

$$\ln \frac{P_1}{P_2} = 2N$$

$$N = \frac{1}{2} \ln \frac{P_1}{P_2}$$

Let us assume the cascade n/w:



$$N_1 = \ln \frac{V_1}{V_2}$$

$$N_2 = \ln \frac{V_2}{V_3}$$

$$N_n = \ln \frac{V_n}{V_{n+1}}$$

$$N = N_1 + N_2$$

$$N = \ln \left(\frac{V_1}{V_2} \times \frac{V_2}{V_3} \right) = \ln \left(\frac{V_1}{V_3} \right)$$

* Decibel

It is the 10 times of common logarithm of ratio of i/p power to o/p power.

$$D = 10 \log \left(\frac{P_1}{P_2} \right)$$

where,

P_1 = i/p power

$$\ln x = \log_{10} x \times \ln 10$$

Let $x = \frac{P_1}{P_2}$ we get

$$\ln \frac{P_1}{P_2} = \log_{10} \frac{P_1}{P_2} \times \ln 10$$

Put

$$\ln \frac{P_1}{P_2} = 2N$$

$$2N = \frac{D}{10} \times 2.3026$$

$$D = \frac{20N}{2.3026}$$

$$D = 8.686 N$$

i.e. 1 Decibel = 8.686 N

$$N = \frac{1}{8.686} D$$

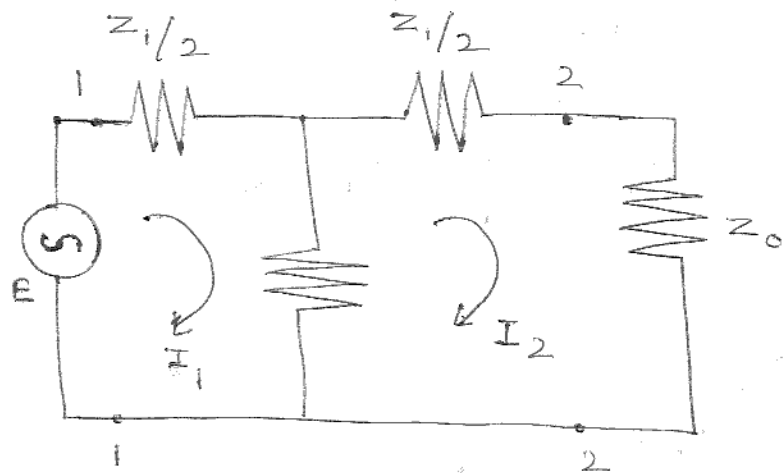
$$N = 0.115 D$$

i.e.

$$1 \text{ Neper} = 0.115 D$$

logar
to

* Properties of Symmetrical Network



$$E = I_1(z_{1/2} + z_2) - I_2 z_2 \quad \text{--- (1)}$$

2nd loop

$$0 = -I_1 z_2 + I_2(z_2 + z_{1/2} + z_0) \quad \text{--- (2)}$$

from eq (2)

$$I_1 z_2 = I_2(z_2 + z_{1/2} + z_0)$$

$$\frac{I_1}{I_2} = \frac{z_2 + z_{1/2} + z_0}{z_2} = e$$

because

$$\frac{I_1}{I_2} = e$$

$$\frac{I_1}{I_2} = e = \frac{z_{1/2}}{z_2} + \frac{z_0}{z_2} + 1 \quad \text{--- (3)}$$

We know that,

$$z_0 = \sqrt{\frac{z_1^2}{4} + z_1 z_2} \quad \text{--- (4)}$$

Substi (4) in (3) we get

$$e^{\gamma} = 1 + \frac{z_1/2}{z_2} + \frac{\sqrt{\frac{z_1^2}{4} + z_1 z_2}}{z_2}$$

$$= 1 + \frac{\frac{z_1}{2}}{z_2} + \sqrt{\frac{\frac{z_1^2}{4}}{4z_2^2} + \frac{z_1}{z_2}} \quad \text{--- (5)}$$

lly,

$$e^{-\gamma} = 1 + \frac{z_1/2}{z_2} - \sqrt{\frac{\frac{z_1^2}{4}}{4z_2^2} + \frac{z_1}{z_2}} \quad \text{--- (6)}$$

Adding eq (5) and eq (6)

$$e^{\gamma} + e^{-\gamma} = 2 + 2 \frac{z_1/2}{z_2} = 2 \left[1 + \frac{z_1/2}{z_2} \right]$$

$$\frac{e^{\gamma} + e^{-\gamma}}{2} = 1 + \frac{z_1/2}{z_2}$$

$$\cos \gamma = 1 + \frac{z_1}{z_2} \quad \text{--- (7)}$$

Subtracting (5) from (6)

$$e^{\gamma} - e^{-\gamma} = 2 \sqrt{\frac{z_1^2}{4z_2^2} + \frac{z_1}{z_2}}$$

$$= \frac{2}{z_2} \sqrt{\frac{z_1^2}{4} + z_1 z_2}$$

$$= \frac{2z_0}{z_2}$$

$$\frac{e^{\gamma} - e^{-\gamma}}{2} = \frac{z_0}{z_2}$$

$$\sinh \gamma = \frac{z_0}{z_2} \quad \text{--- (8)}$$

Dividing (8) by (7)

$$\tanh \gamma = \frac{\sinh \gamma}{\cosh \gamma} = \frac{z_0/z_2}{1 + \frac{z_1}{z_2}}$$

$$\tanh \gamma = \frac{z_0}{z_2 + \frac{z_1}{2}}$$

Consider eq (7)

$$\cosh \gamma = 1 + \frac{z_1/2}{z_2}$$

$$\cosh \gamma - 1 = \frac{z_1}{2z_2}$$

We know that

$$2 \sinh^2 \frac{\gamma}{2} = \cosh \gamma - 1$$

$$\therefore 2 \sinh^2 \frac{\gamma}{2} = \frac{z_1}{2z_2}$$

$$\sinh^2 \frac{\gamma}{2} = \frac{z_1/2}{2z_2}$$

$$\sinh \frac{\gamma}{2} = \sqrt{\frac{z_1/2}{2z_2}}$$

Consider eq (8)

$$\sinh \gamma = \frac{z_0}{z_2}$$

$$2 \sinh \frac{\gamma}{2} \cosh \frac{\gamma}{2} = \frac{z_0}{z_2}$$

$$\cosh \frac{\gamma}{2} = \frac{z_0}{2z_2 \sinh \frac{\gamma}{2}}$$

$$= \frac{z_0}{2z_2} \sqrt{\frac{2z_2}{z_1}} \cdot \frac{1}{2}$$

$$\cosh \frac{\gamma}{2} = \frac{z_0}{\sqrt{\frac{2z_1 z_2}{2}}}$$

$$\tanh \frac{\gamma}{2} = \frac{\sinh \frac{\gamma}{2}}{\cosh \frac{\gamma}{2}}$$

$$= \frac{\sqrt{\frac{z_1/2}{2z_2}}}{\frac{z_0}{\sqrt{2 \frac{z_1}{2} z_2}}}$$

$$= \sqrt{\frac{z_1/2}{2z_2}} \times \frac{\sqrt{2z_1/2 z_2}}{z_0}$$

$$= \sqrt{\frac{z_1/2 \times 2z_1/2 z_2}{2z_2 \times z_0 \times z_0}}$$

$$\tanh \frac{\gamma}{2} = \frac{z_1}{z_0}$$