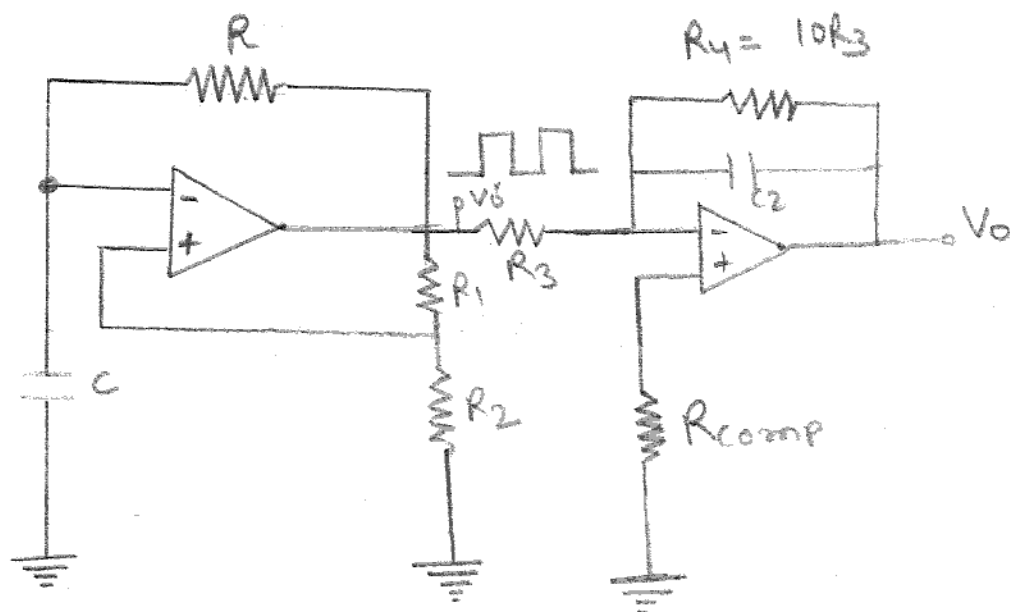


Triangular Wave Generator

A triangular wave can be simply obtained by integrating a square wave as shown in fig(a). It is obvious that the square wave and triangular wave is the same in fig(b). Although the amplitude of the square wave is constant at $\pm V_{sat}$ the amplitude of the triangular wave will decrease as the frequency increases. This is because the reactance of the capacitor C_2 in the feedback circuit decreases at high frequencies. A resistance R_4 is connected across C_2 to avoid the saturation problem at low frequencies as in the case of practical integrator.



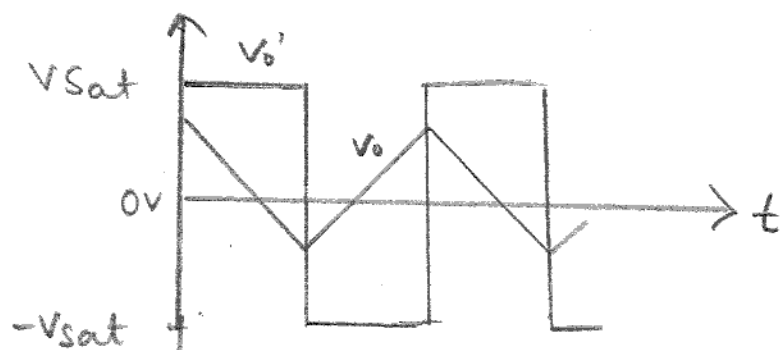
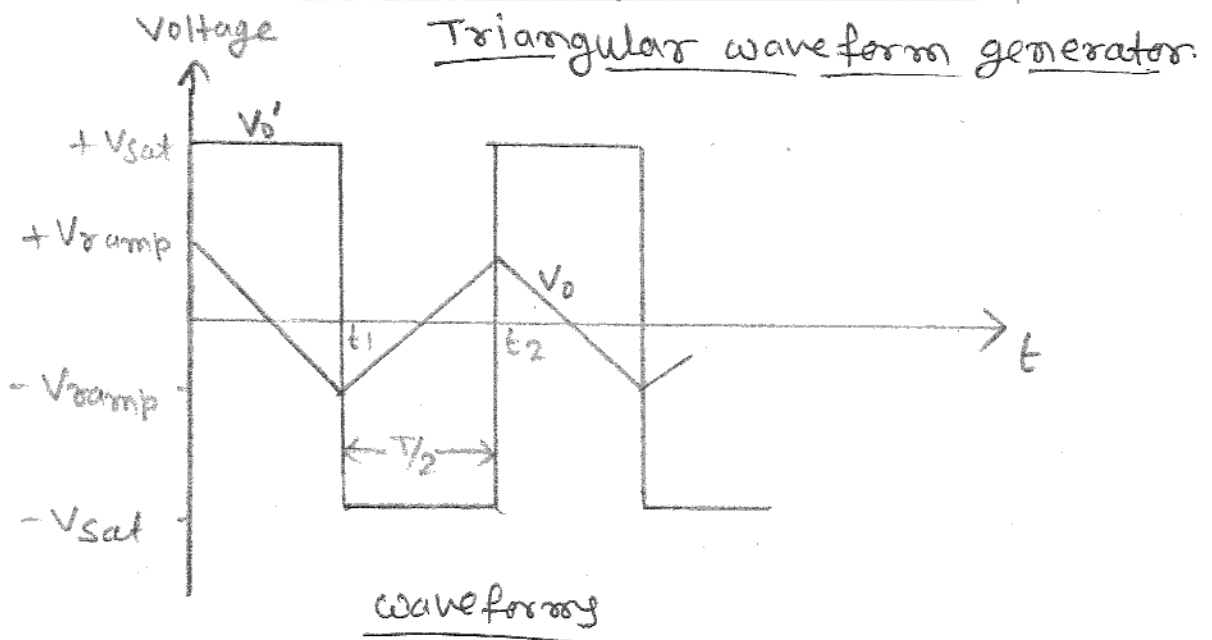
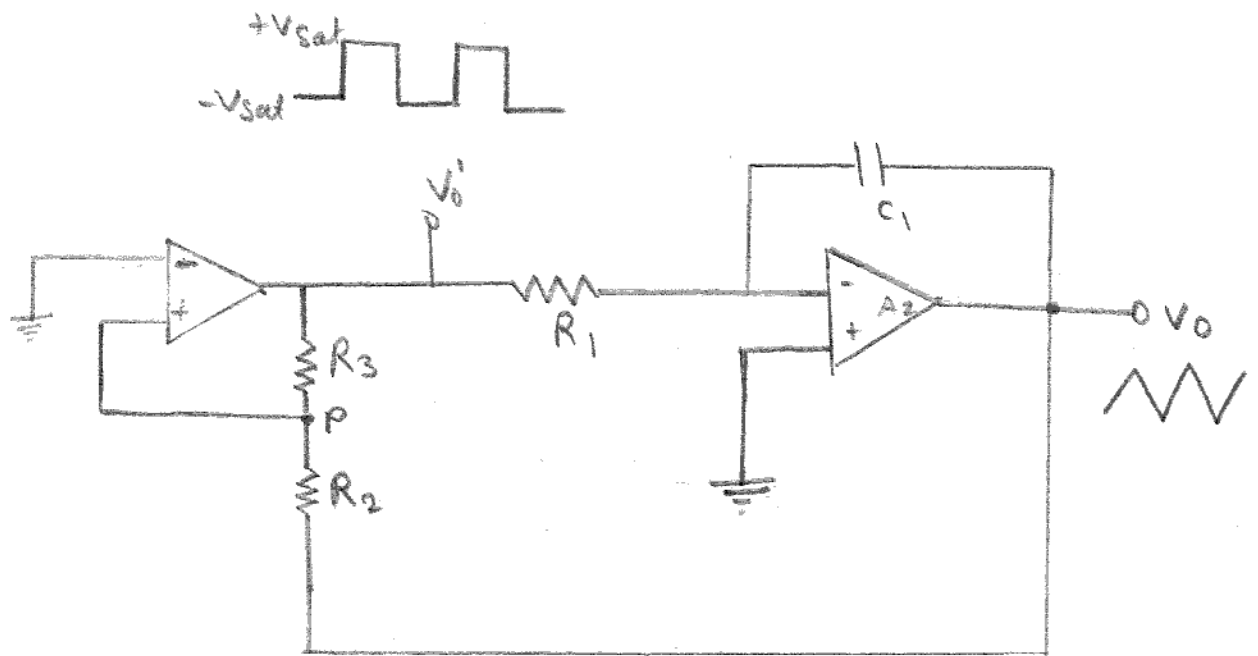


Fig (b) output waveform

Another triangular wave generator using lesser number of components is shown in above fig. It basically consists of a two level comparator followed by an integrator. The output of comparator A_1 is a square wave of amplitude $\pm V_{sat}$ and is applied to the (-) input terminal of the integrator A_2 producing a triangular wave. This triangular wave is fed back as input to the comparator A_1 through a voltage divider $R_2 R_3$.

initially, let us consider that the output of comparator A_1 is at $+V_{sat}$. The output of the integrator A_2 will be a negative going ramp as shown in fig. Thus one end of the voltage divider $R_2 R_3$ is at a voltage $+V_{sat}$ and the other at the negative going ramp of A_2 . At a time $t = t_1$, when the negative going ramp attains a value of $-V_{ramp}$ the effective voltage at point P becomes slightly less than 0V. This switches the output of A_1 from positive saturation to negative saturation level $-V_{sat}$. During the time

when the output of A_1 is at $-V_{sat}$, the output of A_2 increases in the positive direction. And at the instant $t=t_2$, the output of A_2 voltage at point P becomes just above 0V, thereby switching the output of A_1 from $-V_{sat}$ to $+V_{sat}$. The cycle repeats and generates a triangular waveform.



The effective voltage at point P during the time when output of A_1 is at $+V_{sat}$ level is given by

$$-V_{ramp} + \frac{R_2}{R_2 + R_3} [+V_{sat} - (-V_{ramp})] \quad \text{--- (1)}$$

At $t = t_1$, the voltage at point P becomes equal to zero, Therefore

$$-V_{ramp} = -\frac{R_2}{R_3} (+V_{sat}) \quad \text{--- (2)}$$

Similarly at $t = t_2$ when the output of A_1 switches from $-V_{sat}$ to V_{sat} :

$$\begin{aligned} V_{ramp} &= -\frac{R_2}{R_3} (-V_{sat}) \\ &= \frac{R_2}{R_3} (V_{sat}) \quad \text{--- (3)} \end{aligned}$$

Therefore peak to peak amplitude of the triangular wave is

$$\begin{aligned} V_o(PP) &= +V_{ramp} - (-V_{ramp}) \\ &= 2 \frac{R_2}{R_3} V_{sat} \quad \text{--- (4)} \end{aligned}$$

The output switches from $-V_{ramp}$ to $+V_{ramp}$ in half the time period $T/2$ putting the values in the basic integrator equation

$$V_o = -\frac{1}{R_1 C} \int V_i dt$$

$$V_o(\text{PP}) = -\frac{1}{R_1 C_1} \int_0^{T/2} (-V_{\text{sat}}) dt$$

$$= \frac{V_{\text{sat}}}{R_1 C_1} \left(\frac{T}{2} \right)$$

$$\Rightarrow T = 2 R_1 C_1 \frac{V_o(\text{PP})}{V_{\text{sat}}} \quad \text{--- (5)}$$

Putting the value of $V_o(\text{PP})$ from eq. (4)

$$T = \frac{4 R_1 C_1 R_2}{R_3}$$

Hence the frequency of oscillation f_o is

$$f_o = \frac{1}{T} = \frac{R_3}{4 R_1 R_2 C_1}$$

(2)

LOG AMPLIFIER AND ANTILOG AMPLIFIER

There are several applications of log and antilog amplifier. Antilog computation may require functions such as $\ln x$, $\log x$ or $\sin x$.

These can be performed continuously with log-amps. One would like to have direct dB display on digital voltmeter and spectrum analyser. Log-amp can be easily perform this function. Log-amp can also used to compress the dynamic range of a signal.

LOG AMPLIFIER

The fundamental log-amp circuit in Fig. (a) where a grounded base transistor is placed in the feedback path. Since the collector is held at virtual ground and the base is also grounded, the transistor's voltage-current relationship becomes that of a diode and is given by.

$$I_E = I_S (e^{qV_E/KT} - 1) \quad \text{--- (1)}$$

Since $I_C = I_B$ for a grounded base transistor.

$$I_C = I_S (e^{qV_E/KT} - 1) \quad \text{--- (2)}$$

I_S = emitter saturation current $\approx 10^{-13}$ A

k = Boltzmann's constant

T = absolute temperature ($^{\circ}\text{K}$)

$$\text{Therefore } \frac{I_C}{I_S} = (e^{qV_E/KT} - 1) \quad \text{--- (3)}$$

$$\text{or } e^{qV_E/KT} = \frac{I_C}{I_S} + 1$$

$$\approx \frac{I_C}{I_S} \quad [\text{as } I_S \approx 10^{-13} \text{ A, } I_C \gg I_S]$$

Taking natural log on both sides, we get

$$V_E = \frac{KT}{q} \ln \left(\frac{I_C}{I_S} \right) \quad \text{--- (4)}$$

$$\therefore I_C = \frac{V_i}{R_i}$$

$$V_E = -V_O$$

$$\text{So, } V_O = -\frac{KT}{q} \ln\left(\frac{V_i}{R_1 I_S}\right) = -\frac{KT}{q} \ln\left(\frac{V_i}{V_{ref}}\right)$$

where. $V_{ref} = R_1 I_S$

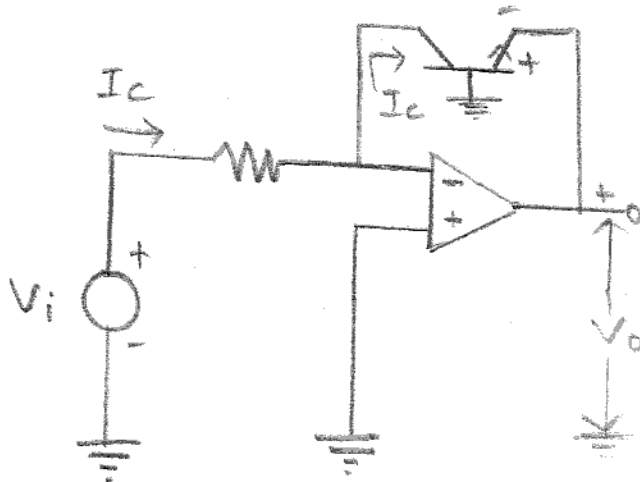


Fig. (a) Fundamental log-amp circuit.

The output voltage is thus proportional to the logarithm of input voltage. Although the ckt gives natural $\log(I_m)$. one can find \log_{10} by proper scaling.

$$\log_{10} X = 0.4343 \ln X$$

The circuit, however, has one problem. The emitter saturation current I_S varies from transistor to transistor and with temperature. Thus a stable reference voltage V_{ref} cannot be obtained. This is eliminated by the ckt given in Fig-4.18(b). The input is applied to

one log-amp, while a reference voltage is applied to another log-amp. The two transistors are integrated close together on the same silicon wafer. This provides a close match of saturation currents and ensures good thermal tracking.

Assume $I_{S1} = I_{S2} = I_S$

and then

$$V_1 = \frac{KT}{q} \ln\left(\frac{V_i}{R_1 I_S}\right)$$

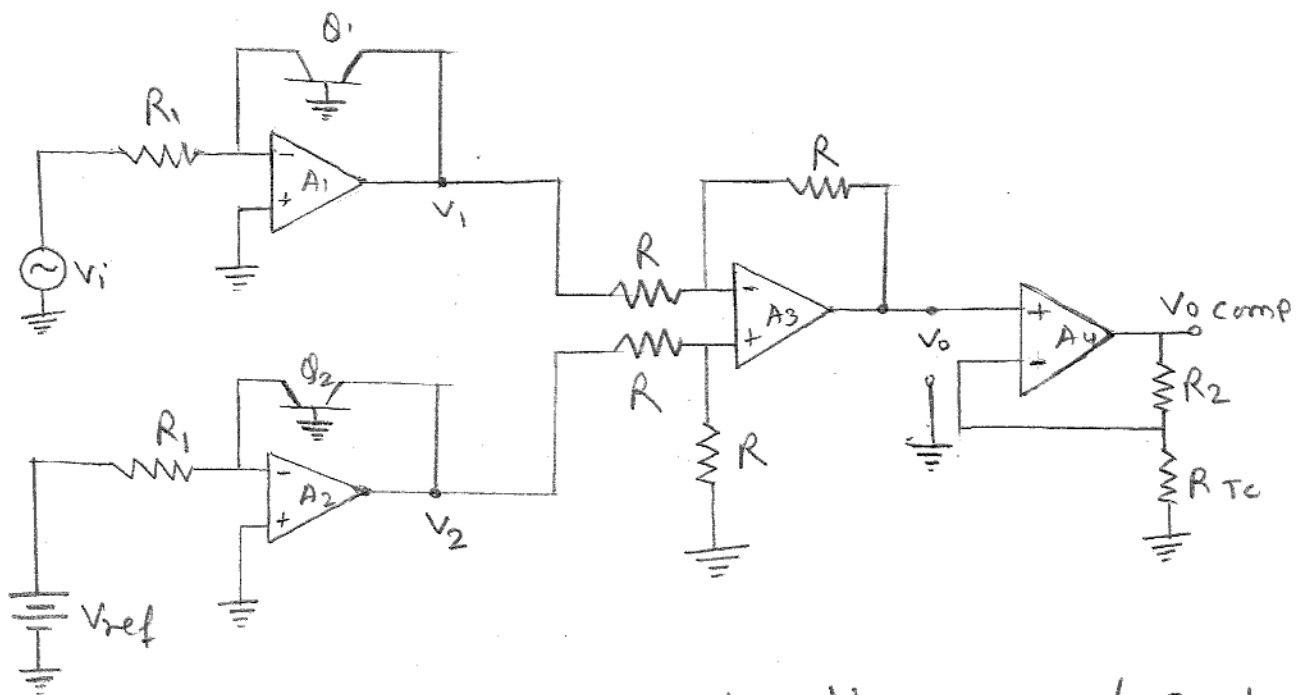


Fig. Log-amp with saturation current and temperature compensation.

and $V_2 = -\frac{KT}{q} \ln\left(\frac{V_{ref}}{R_1 I_S}\right)$

$$V_0 = V_2 - V_1 = \frac{KT}{q} \left[\ln\left(\frac{V_i}{R_1 I_S}\right) - \ln\left(\frac{V_{ref}}{R_1 I_S}\right) \right]$$

$$V_0 = \frac{KT}{q} \ln\left(\frac{V_i}{V_{ref}}\right)$$

Antilog Amplifier

In this ckt the input V_i for the antilog. amp is fed into the temperature compensating voltage divider R_2 and R_{TC} and then to the base of Q_2 . The output V_o of the antilog. amp is fed back to the inverting input of A_1 through the resistor R_1 . The base to emitter voltage of transistors Q_1 and Q_2 can be written as

$$V_{Q_1 \text{ B-E}} = \frac{kT}{q} \ln \left(\frac{V_o}{R_1 I_s} \right)$$

$$\text{and } V_{Q_2 \text{ B-E}} = \frac{kT}{q} \ln \left(\frac{V_{ref}}{R_1 I_s} \right)$$

Since the base of Q_1 is tied to ground, we get

$$V_A = -V_{Q_1 \text{ B-E}} = -\frac{kT}{q} \ln \left(\frac{V_o}{I_s R_1} \right)$$

the ^{base} voltage V_B of Q_2 is

$$V_B = \left(\frac{R_{TC}}{R_2 + R_{TC}} \right) V_i$$

The voltage at the emitter of Q_2 is

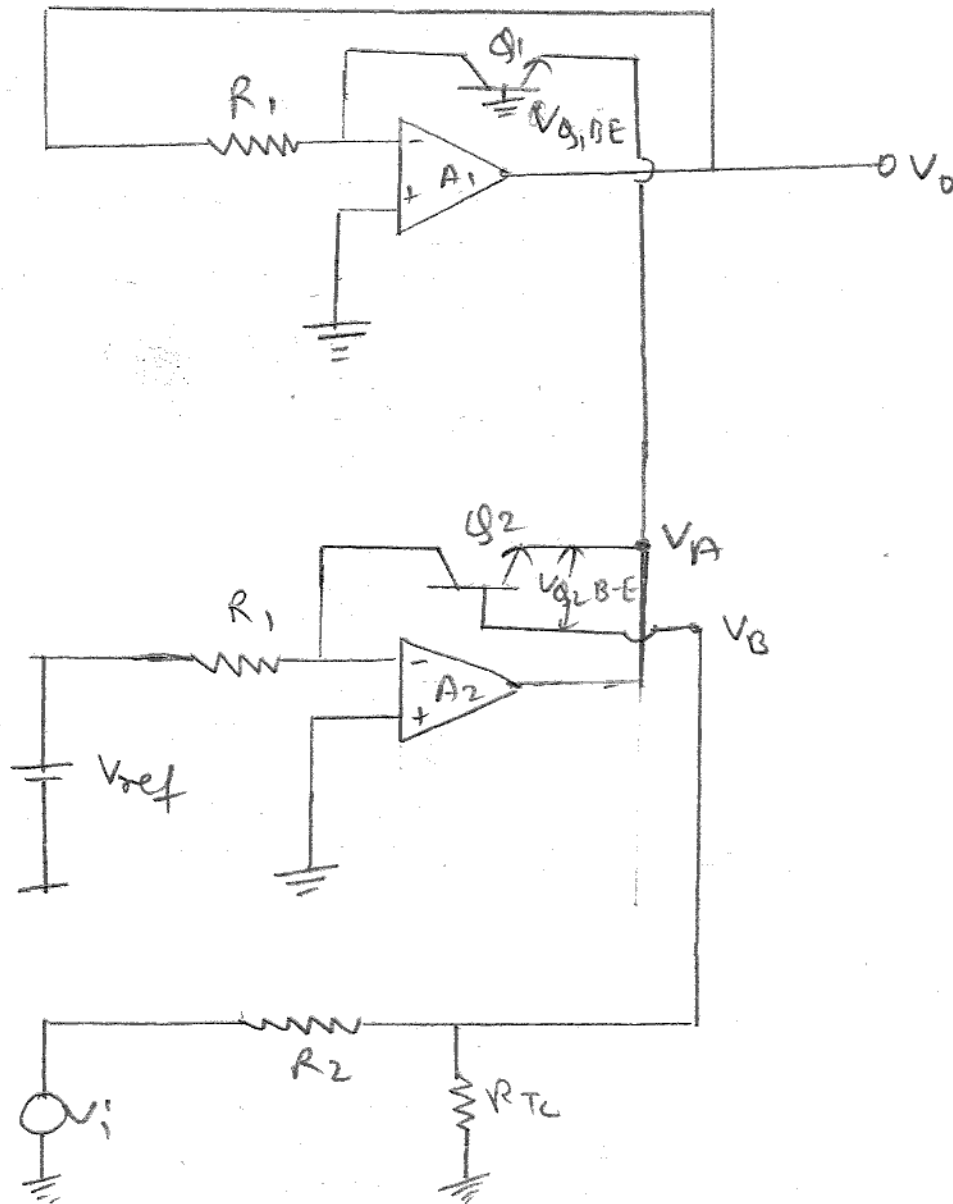
$$V_{Q_2 E} = V_B + V_{Q_2 \text{ B-E}}$$

$$\text{or } V_{Q_2 E} = \left(\frac{R_{TC}}{R_2 + R_{TC}} \right) V_i - \frac{kT}{q} \ln \left(\frac{V_{ref}}{R_1 I_s} \right)$$

But the emitter voltage of Q_2 is V_A that is

$$V_A = V_{Q_2 E}$$

$$-\frac{KT}{e} \ln \frac{V_0}{R_1 I_S} = \frac{R_{TC}}{R_2 + R_{TC}} V_i - \frac{KT}{e} \ln \frac{V_{ref}}{R_1 I_S}$$



ANITLON AMP.

$$\Rightarrow \frac{R_{TC}}{R_2 + R_{TC}} V_i = -\frac{KT}{e} \left(\ln \frac{V_0}{R_1 I_S} - \ln \frac{V_{ref}}{R_1 I_S} \right)$$

$$= -\frac{e}{KT} \cdot \frac{R_{TC}}{R_2 + R_{TC}} V_i = \ln \left(\frac{V_0}{V_{ref}} \right)$$

changing natural log, i.e. \ln to \log_{10} using

$$-0.4343 \left(\frac{q}{kT} \right) \left(\frac{R_{TC}}{R_2 + R_{TC}} \right) v_i = 0.4343 \times \ln \left(\frac{V_o}{V_{ref}} \right)$$

$$-k' v_i = \log_{10} \left(\frac{V_o}{V_{ref}} \right)$$

or
$$\frac{V_o}{V_{ref}} = 10^{-k' v_i}$$

$$V_o = V_{ref} (10^{-k' v_i})$$

where $k' = 0.4343 \left(\frac{q}{kT} \right) \left(\frac{R_{TC}}{R_2 + R_{TC}} \right)$